

Unit 2 Applications of Equations and Inequalities
4.5 Compound Inequalities DAY 1

Day _____

I can . . .

. . . graph and write inequalities containing “*and*” and “*or*”.

Pick a number that is greater than 5 or less than or equal to -1.

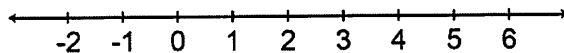
Pick a number that is less than or equal to 5 and less than -1.

Pick a number that is greater than 5 and less than -1.

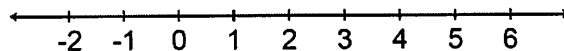
A **Compound Inequality** is two inequalities that are joined by the word **and** or the word **or**.

OR

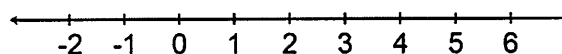
$$x > 5 \text{ or } x \leq -1$$



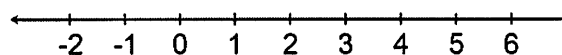
$$x \geq 5 \text{ or } x < -1$$



$$x \geq 5 \text{ or } x \leq -1$$



$$x > 5 \text{ or } x < -1$$



AND

Set-Builder Notation

$$-1 \leq x < 5$$

or

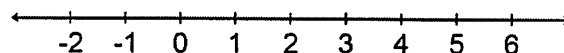
Interval Notation

$$[-1, 5)$$

$$x < 5 \text{ and } x \geq -1$$

$$-1 \leq x < 5$$

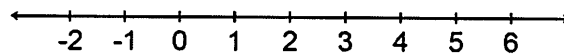
$$[-1, 5)$$



$$x \leq 5 \text{ and } x > -1$$

$$-1 < x \leq 5$$

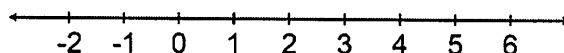
$$(-1, 5]$$



$$x \leq 5 \text{ and } x \geq -1$$

$$-1 \leq x \leq 5$$

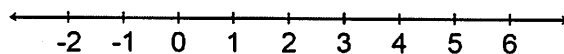
$$[-1, 5]$$



$$x < 5 \text{ and } x > -1$$

$$-1 < x < 5$$

$$(-1, 5)$$



I THINK I GOT IT?

Write a compound inequality, in set-builder and interval notation (and statements only), that represents each situation. Graph the solutions.

1. All real numbers that are at least -1 and at most 3.
2. All real numbers that are less than 0 or greater than or equal to 6.
3. All real numbers that are less than -1, but greater than -5

I GOT IT!

4. Discounted tickets are available to children under 7 years old or to adults 65 and older.
5. Fun Night is for all students who are at most 14 years old and at least 10 years old.

(1) $-1 \leq x \leq 3$ (2) $x < 0$ or $x \geq 6$ (3) $-5 < x < -1$ (4) $x > 7$ or $x \geq 65$ (5) $10 \leq x \leq 14$ [10, 14]

Practice: p229 1-4 and p230 17-20, 29-32

Unit 2 Applications of Equations and Inequalities
4.5 Compound Inequalities DAY 2

Day _____

I can . . .

. . . solve compound inequalities.

Is 3 the solution to the inequality: $-2(x + 5) \geq 5x + 23$?

Is 3 the solution to the compound inequality: $-(x - 8) < 9$ and $\frac{x}{5} + 1 \leq 2$?

Solve the compound inequality and graph the solution.

$$-3 \leq \frac{3}{2}x + 6 \leq 3$$

$$7 + 2a > 9 \text{ or } -4a > 8$$

I GOT IT!

$$t + 5 < 2 \text{ or } 3t + 1 > 10$$

$$-29 \leq 5s - 4 \leq 41$$

Practice: p230 7, 9, 15, 25, 27 and p231 43, 46-48

Unit 2 Applications of Equations and Inequalities

Day _____

4.5 Compound Inequalities DAY 1

I can . . .

. . . graph and write inequalities containing "and" and "or".

Pick a number that is greater than 5 or less than or equal to -1.



A value that satisfies one or the other inequality

Pick a number that is less than or equal to 5 and less than -1.

0

A value that satisfies both inequalities

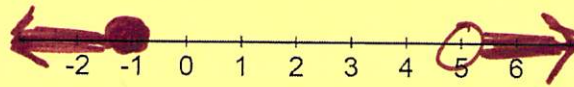
Pick a number that is greater than 5 and less than -1.

There is no value that satisfies both inequalities at the same time.

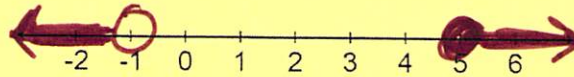
A **Compound Inequality** is two inequalities that are joined by the word **and** or the word **or**.

OR

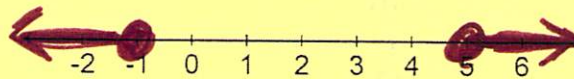
$x > 5$ or $x \leq -1$



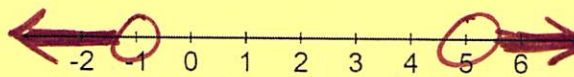
$x \geq 5$ or $x < -1$



$x \geq 5$ or $x \leq -1$



$x > 5$ or $x < -1$



AND

Set-Builder Notation

or

Interval Notation

$-1 \leq x < 5$

$[-1, 5)$

$x < 5$ and $x \geq -1$

$-1 \leq x < 5$

$[-1, 5)$



$x \leq 5$ and $x > -1$

$-1 < x \leq 5$

$(-1, 5]$



$x \leq 5$ and $x \geq -1$

$-1 \leq x \leq 5$

$[-1, 5]$



$x < 5$ and $x > -1$

$-1 < x < 5$

$(-1, 5)$



I THINK I GOT IT?

Write a compound inequality, in set-builder and interval notation (and statements only), that represents each situation. Graph the solutions.

1. All real numbers that are at least -1 **and** at most 3.

$$x \geq -1 \quad x \leq 3$$

$$\{x \mid -1 \leq x \leq 3\}$$

$$[-1, 3]$$

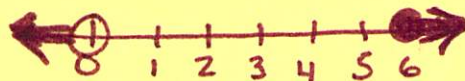


2. All real numbers that are less than 0 **or** greater than or equal to 6.

$$x < 0 \quad x \geq 6$$

$$\{x \mid x < 0 \text{ or } x \geq 6\}$$

$$(-\infty, 0) \cup [6, \infty)$$



3. All real numbers that are less than -1, but greater than -5

$$x < -1 \text{ and } x > -5$$

$$-5 < x < -1$$

$$(-5, -1)$$



I GOT IT!

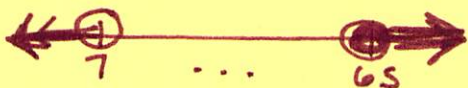
4. Discounted tickets are available to children under 7 years old or to adults 65 and older.

$$\{x \mid x < 7 \text{ or } x \geq 65\}$$

$$(0, 7) \cup [65, \infty)$$

$$a < 7$$

$$\text{or } a \geq 65$$



5. Fun Night is for all students who are at most 14 years old **and** at least 10 years old.

$$a \leq 14$$

$$a \geq 10$$

$$\{x \mid 10 \leq x \leq 14\}$$

$$[10, 14]$$



(1) $-1 \leq x \leq 3$ (2) $x < 0$ or $x \geq 6$ (3) $-5 < x < -1$ (4) $x > 7$ or $x \geq 65$ (5) $10 \leq x \leq 14$ (6) $[10, 14]$

Unit 2 Applications of Equations and Inequalities

4.5 Compound Inequalities DAY 2

Day _____

I can ...

... solve compound inequalities.

Is 3 the solution to the inequality: $-2(x+5) \geq 5x+23$?

Solve

$$\begin{array}{r} -2x - 10 \geq 5x + 23 \\ +2x \quad +2x \end{array}$$

$$\begin{array}{r} -10 \geq 7x + 23 \\ -23 \quad -23 \end{array}$$

$$\frac{-33}{7} \geq \frac{7x}{7}$$

$$-4\frac{5}{7} \geq x$$

NO

$$-4\frac{5}{7} \not\geq 3$$

Plug - In

$$-2(3+5) \geq 5(3)+23$$

$$-2(8) \geq 15+23$$

$$-16 \not\geq 38$$

NO

Is 3 the solution to the compound inequality: $-(x-8) < 9$ and $\frac{x}{5} + 1 \leq 2$?

BOTH

$$\begin{array}{r} -x + 8 < 9 \\ -8 \quad -8 \end{array}$$

$$\begin{array}{r} -x < 1 \\ -1 \quad -1 \end{array}$$

$$x > -1$$

Yes

$$3 > -1$$

$$\begin{array}{r} \frac{x}{5} + 1 \leq 2 \\ -1 \quad -1 \end{array}$$

$$\text{AND } 5 \cdot \frac{x}{5} \leq 1 \cdot 5$$

$$x \leq 5$$

Yes

$$3 \leq 5$$

YES

Solve the compound inequality and graph the solution.

$$-3 \leq \frac{3}{2}x + 6 \leq 3$$

$$-6 \quad -6 \quad -6$$

$$\frac{2}{3} \cdot -9 \leq \frac{3}{2}x \leq -3 \cdot \frac{2}{3}$$
$$\cdot \frac{2}{3}$$

$$-6 \leq x \leq -2$$

$$[-6, -2]$$



$$7 + 2a > 9 \text{ or } -4a > 8$$

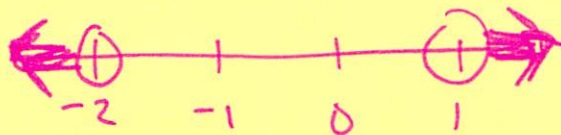
$$-7 \quad -7 \quad -4 \quad -4$$

$$\frac{2a > 2}{2 \quad 2} \quad a < -2$$

$$a > 1$$

$$a > 1 \text{ or } a < -2$$

$$(-\infty, -2) \cup (1, \infty)$$



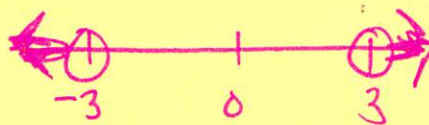
I GOT IT!

$$t + 5 < 2 \text{ or } 3t + 1 > 10$$

$$\begin{array}{r} -5 \quad -5 \quad -1 \quad -1 \\ t < -3 \quad \frac{3t}{3} > \frac{9}{3} \\ t < -3 \quad t > 3 \end{array}$$

$$t < -3 \text{ or } t > 3$$

$$(-\infty, -3) \cup (3, \infty)$$



$$-29 \leq 5s - 4 \leq 41$$

$$\begin{array}{r} +4 \quad +4 \quad +4 \\ -29 \leq 5s - 4 \leq 41 \end{array}$$

$$\frac{-29}{5} \leq \frac{5s}{5} \leq \frac{45}{5}$$

$$-5 \leq s \leq 9$$

$$[-5, 9]$$

