

"I Can Identify the Properties of Math that Generate Equivalent Expressions."

Commutative and Associative Properties

Two or more **Like Terms** are able to be simplified into a single term. If terms are **Unlike** then they cannot be combined.

Examples:

$4e + 2e$	$d^3 \bullet d^2$	$2x + 4$
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Use the idea of Combining Like Terms to Simplify the following expressions

$4 \bullet 2 \bullet m \bullet m$	$b + b + b + 2 + 7$	$8 - 2 + 7 + x + x$
$3a + 6a - 9$	$a + 5a + 8 - 9$	$2a + 4a + 5b + 2b$

Commutative Property

For which operations can we move around the numbers and still get the same answer?

$2 + 6 + 8$ and $8 + 6 + 2$	$12 - 5 - 2$ and $5 - 12 - 2$
$6 \bullet 4$ and $4 \bullet 6$	$8 \div 2$ and $2 \div 8$

OK but what if we use both addition and multiplication.

$2 + 4 \bullet 3$ and $3 + 2 \bullet 4$

Use the **Commutative Property** to combine like terms and simplify each expression.

1)	$3 \bullet g \bullet 4$	2)	$a + b + a + b + a$
3)	$3 \bullet 3 \bullet d \bullet 2 \bullet d \bullet d$	4)	$2a + 4 + 6 + 3a$
5)	$2x + 3y + 2x + 9 + 7y$	6)	$3 \bullet p \bullet p \bullet q \bullet 5 \bullet q \bullet p$

Associative Property

This property states you can change the grouping of the numbers within addition and multiplication expressions and still maintain equivalency.

$2 + (6 + 8)$ and $(2 + 6) + 8$	$(5 \bullet 3) \bullet 2$ and $5 \bullet (3 \bullet 2)$
Notice the Order of the Numbers doesn't change!	Notice the Order of the Numbers doesn't change!

Examples: Write an equivalent expression using the associative property.

1) $(a + b) + c$

2) $8 \bullet (7 \bullet 9)$

3) $3 \bullet (1 \bullet 8) \bullet 2$

4) $(2e + 5e) + 7e$

"I Can Identify the Properties of Math that Generate Equivalent Expressions."

Commutative and Associative Properties

Two or more **Like Terms** are able to be simplified into a single term. If terms are **Unlike** then they cannot be combined.

Examples:

$\begin{array}{c} 4e + 2e \\ \underbrace{e+e+e+e+e+e} \\ 6e \end{array}$	$\begin{array}{c} d^3 \cdot d^2 \\ \underbrace{d \cdot d \cdot d \cdot d \cdot d} \\ d^5 \end{array}$	$\begin{array}{c} 2x + 4 \\ \underbrace{x + x + 4} \\ 2x + 4 \end{array}$ <p style="text-align: right;">CAN'T COMBINE</p>
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Use the idea of Combining Like Terms to Simplify the following expressions

$\begin{array}{c} 4 \cdot 2 \cdot m \cdot m \\ \underbrace{4 \cdot 2} \quad \underbrace{m \cdot m} \\ 8 \cdot m^2 \end{array}$	$\begin{array}{c} b + b + b + 2 + 7 \\ \underbrace{b + b + b} \\ 3b + 9 \end{array}$	$\begin{array}{c} 8 - 2 + 7 + x + x \\ \underbrace{8 - 2 + 7} \quad \underbrace{x + x} \\ 13 + 2x \end{array}$
$\begin{array}{c} 3a + 6a - 9 \\ \underbrace{3a + 6a} \\ 9a - 9 \end{array}$	$\begin{array}{c} a + 5a + 8 - 9 \\ \underbrace{a + 5a} \quad \underbrace{8 - 9} \\ 6a - 1 \end{array}$	$\begin{array}{c} 2a + 4a + 5b + 2b \\ \underbrace{2a + 4a} \quad \underbrace{5b + 2b} \\ 6a + 7b \end{array}$

Commutative Property

For which operations can we move around the numbers and still get the same answer?

$\begin{array}{c} * \\ 2 + 6 + 8 \quad \text{and} \quad 8 + 6 + 2 \\ \underbrace{2 + 6} \quad \underbrace{8 + 8} \quad \underbrace{14 + 2} \\ 8 + 8 \quad 16 \quad 16 \end{array}$	 $\begin{array}{c} 12 - 5 - 2 \quad \text{and} \quad 5 - 12 - 2 \\ \underbrace{12 - 5} \quad \underbrace{-7 - 2} \\ 7 - 2 \quad -9 \end{array}$
$\begin{array}{c} * \\ 6 \cdot 4 \quad \text{and} \quad 4 \cdot 6 \\ \underbrace{6 \cdot 4} \quad \underbrace{4 \cdot 6} \\ 24 \quad 24 \end{array}$	 $\begin{array}{c} 8 \div 2 \quad \text{and} \quad 2 \div 8 \\ \underbrace{8 \div 2} \quad \underbrace{2 \div 8} \\ 4 \quad \frac{1}{4} \end{array}$

OK but what if we use both addition and multiplication.

 $\begin{array}{c} 2 + 4 \cdot 3 \quad \text{and} \quad 3 + 2 \cdot 4 \\ \underbrace{2 + 4} \quad \underbrace{3 + 8} \\ 6 + 3 \quad 11 \end{array}$

Use the **Commutative Property** to combine like terms and simplify each expression.

1) $3 \cdot g \cdot 4$ $3 \cdot 4 = g$ $12 \cdot g$	2) $a + b + a + b + a$ $a + a + a + b + b$ $3a + 2b$
3) $3 \cdot 3 \cdot d \cdot 2 \cdot d \cdot d$ $3 \cdot 3 = 2 \cdot d \cdot d \cdot d$ $18 \cdot d^3$	4) $2a + 4 + 6 + 3a$ $2a + 3a + 4 + 6$ $5a + 10$
5) $2x + 3y + 2x + 9 + 7y$ $2x + 2x + 3y + 7y + 9$ $4x + 10y + 9$	6) $3 \cdot p \cdot p \cdot q \cdot 5 \cdot q \cdot p$ $3 \cdot 5 \cdot p \cdot p \cdot p \cdot q \cdot q$ $15 \cdot p^3 \cdot q^2$

Associative Property

This property states you can change the grouping of the numbers within addition and multiplication expressions and still maintain equivalency.

$2 + (6 + 8)$ and $(2 + 6) + 8$ $2 + 14$ $8 + 8$ 16 16	$(5 \cdot 3) \cdot 2$ and $5 \cdot (3 \cdot 2)$ $15 \cdot 2$ $5 \cdot 6$ 30 30
Notice the Order of the Numbers doesn't change!	Notice the Order of the Numbers doesn't change!

Examples: Write an equivalent expression using the associative property.

1) $(a + b) + c$

$a + (b + c)$

2) $8 \cdot (7 \cdot 9)$

$(8 \cdot 7) \cdot 9$

3) $3 \cdot (1 \cdot 8) \cdot 2$

$(3 \cdot 1) \cdot 8 \cdot 2$

4) $(2e + 5e) + 7e$

$2e + (5e + 7e)$