

# Solving Rational Equations Part Two

Sometimes you will come across a difficult Rational Equation to solve where your strategies just won't work. Let's take a look at some equations that contain some fractions. In the end, we are still trying to solve for  $x$ . To do this we need to follow two steps:

1. Get Common Denominators (**Least Common Multiple**)
2. Solve **JUST** the equation located in the numerator for the variable

$$\frac{\boxed{3}}{\cancel{10}} + \frac{\boxed{6}}{\cancel{10}} = \frac{\boxed{9}}{\cancel{10}}$$

$$\frac{\boxed{8x}}{\cancel{13}} - \frac{\boxed{4x}}{\cancel{13}} = \frac{\boxed{4x}}{\cancel{13}}$$

These equations can't be solved for  $x$ , but let's look at some that can!

1.  $\frac{3x+1}{\cancel{12}} + \frac{7}{\cancel{12}} = \frac{7x}{\cancel{12}}$

$$3x + 1 + 7 = 7x$$

$$\begin{array}{r} 3x + 8 = 7x \\ -3x \quad -3x \\ \hline \end{array}$$

$$\frac{8}{4} = \frac{4x}{4}$$

$$x = 2$$

2.  $\frac{3}{3} \cdot \frac{2x}{5} + \frac{1}{3} \cdot \frac{7x-2}{5} = \frac{7x-2}{15}$

$$\frac{6x}{\cancel{15}} + \frac{5}{\cancel{15}} = \frac{7x-2}{\cancel{15}}$$

$$\begin{array}{r} 6x + 5 = 7x - 2 \\ -6x \quad -6x \\ \hline \end{array}$$

$$\begin{array}{r} 5 = x - 2 \\ +2 \quad +2 \\ \hline \end{array}$$

$$7 = x$$

$$3. \frac{2}{2} \cdot \frac{x}{3} + \frac{(x+1)^3}{2 \cdot 3} \cdot \frac{x}{1} \cdot \frac{6}{6}$$

$$\frac{2x}{6} + \frac{3x+3}{6} = \frac{6x}{6}$$

$$2x + 3x + 3 = 6x$$

$$\begin{array}{r} 5x + 3 = 6x \\ -5x \quad \quad -5x \end{array}$$

$$\boxed{3 = x}$$

$$4. \frac{m}{5} + \frac{3(m-1)}{2} = \frac{2(m-3)}{10}$$

$$\frac{2}{2} \cdot \frac{m}{5} + \frac{5 \cdot (3m-3)}{5 \cdot 2} = \frac{(2m-6) \cdot 10}{1 \cdot 10}$$

$$\frac{2m}{10} + \frac{15m-15}{10} = \frac{20m-60}{10}$$

$$\begin{array}{r} 2m + 15m - 15 = 20m - 60 \\ \hline 17m - 15 = 20m - 60 \end{array}$$

$$\begin{array}{r} 17m - 15 = 20m - 60 \\ -17m \quad \quad -17m \end{array}$$

$$\begin{array}{r} -15 = 3m - 60 \\ +60 \quad \quad +60 \end{array}$$

$$\frac{45}{3} = \frac{3m}{3}$$

$$\boxed{15 = m}$$

$$5. \frac{3}{4} = \frac{-(x+11)}{4x} + \frac{1}{2x}$$

$$\frac{x}{x} \cdot \frac{3}{4} = \frac{-x-11}{4x} + \frac{1}{2x} \cdot \frac{2}{2}$$

$$\frac{3x}{4x} = \frac{-x-11}{4x} + \frac{2}{4x}$$

$$3x = -x - 11 + 2$$

$$\begin{array}{r} 3x = -x - 9 \\ +x \quad \quad +x \end{array}$$

$$\frac{4x}{4} = \frac{-9}{4}$$

$$\boxed{x = -\frac{9}{4}}$$

Solve for  $x$ .

$$1. \quad \frac{x+3}{2} - \frac{x}{5} = \frac{4x+11}{10}$$

$$2. \quad \frac{8}{2x} + 2 = \frac{12}{x}$$

$$3. \quad \frac{5}{x} + \frac{12}{x^2} = \frac{8}{x}$$