

# Introduction to Sets

**Sets** are simply collections of items.

A set may contain your favorite even numbers, the days of the week, or the names of your brothers and sisters. The items contained within a set are called **elements**, and elements in a set do not "repeat".

1. Set Roster – A list of the elements in a set with  $\{\}$  around the elements.

$A = \{2,3,4,5\}$  includes \_\_\_\_\_

$B = \{1,3,5,7,9\}$  includes \_\_\_\_\_

2. Set Builder Notation - A shorthand way of writing elements of a set.

$X = \{x \mid x \text{ is a factor of } 16\}$  includes \_\_\_\_\_  
"x such that x is a factor of 16"

$Y = \{x \mid x \text{ is a multiple of } 3\}$  includes \_\_\_\_\_

**Empty set** \_\_\_\_\_ It is defined by the symbol \_\_\_\_\_

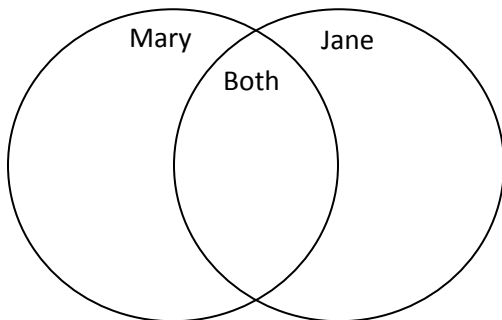
**Universal Set** \_\_\_\_\_

**Complement of a set** \_\_\_\_\_

| Union of Two or More Sets ( $\cup$ ) | Intersection of Two or More Sets ( $\cap$ ) |
|--------------------------------------|---|
|--------------------------------------|---|

Example Problem:

Mary and Jane wanted to paint a picture but could only use the colors of the rainbow. Mary chose orange, blue, purple and green. Jane chose to use red, orange, and blue.



Universal set:

Mary  $\cup$  Jane:

Mary  $\cap$  Jane:

Complement of (Mary  $\cup$  Jane):

# Union

Union ( $\cup$ ) of two or more sets includes **ALL of the elements of ALL of the sets.**

**\*\*The elements in a set do not repeat\*\***

**For Example:**

$$A = \{1,3,5,7,9\} \text{ and } B = \{2,4,6,8,10\}$$

$$A \cup B = \{1,2,3,4,5,6,7,8,9,10\}$$

1. Given:  $Q = \{1,4,6,9\}$

$$R = \{1,3,6,8\}$$

What is the Union of the two sets?

2. Given:  $P = \{\text{Sunday, Monday, Tuesday}\}$

$$O = \{\text{Thursday, Friday, Saturday}\}$$

What is set  $P \cup O$ ?

3. Set A is a set of integers from 0 to 5. Set B is a set of odd integers from 1 to 9.

Find  $A \cup B$ .

4. Given  $Y = \{x \mid x \text{ is a factor of } 8\}$

$$Z = \{x \mid x \text{ is a factor of } 20\}$$

Find  $Y \cup Z$ .

5. Given:  $A = \{J,A,K,E\}$

$$B = \{B,E,T,H,A,N,Y\}$$

$$C = \{T,H,O,M,A,S\}$$

Find the Union of the 3 Sets.

# Intersection

Intersection ( $\cup$ ) of two or more sets includes **where the elements overlap**.

**\*\*The elements in a set do not repeat\*\***

**For Example:**

$$\mathbf{A = \{1,3,5,7,9\} \text{ and } B = \{1,2,3,4,5\}}$$

$$\mathbf{A \cap B = \{1,3,5\}}$$

1. Given:  $M = \{1,4,6,9\}$

$$N = \{1,3,6,8\}$$

What is the Intersection of the two sets?

2. Given:  $D = \{\text{January, March, April, May}\}$

$$L = \{\text{April, May, July, September}\}$$

What is set  $D \cap L$ ?

3. Set A is a set of even integers. Set B is a set of odd integers from 1 to 9.

Find  $A \cap B$ .

4. Given  $G = \{x \mid x \text{ is a factor of } 24\}$

$$O = \{x \mid x \text{ is a factor of } 18\}$$

Find  $G \cap O$ .

5. Given:  $A = \{J,A,K,E\}$

$$B = \{B,E,T,H,A,N,Y\}$$

$$C = \{T,H,O,M,A,S\}$$

Find the Intersection of the 3 Sets.

# Complement

Complement of a set is the **elements that are NOT in the set.**

**\*\*The elements in a set do not repeat\*\***

**For Example:**

**If the universal set  $U = \{0,1,2,3,4,5,6,7,8,9,10\}$**

**and**

**$A = \{1,3,5,7,9\}$**

**$(A)' = \{0,2,4,6,8,10\}$**

1. Given:  $U = \{0 \leq x \leq 10\}$

$N = \{1,3,6,8\}$

If Set  $U$  is the universal set, what is the complement of Set  $N$ ?

2. Given:  $U = \{\text{The 7 days of the week}\}$

$L = \{\text{Monday, Tuesday, Friday}\}$

What is set  $(L)'$ ?

3. Given: Set  $U = \{S,O,P,H,I,A\}$

Set  $B = \{A,I,O\}$

If set  $B$  is a subset of set  $U$ , what is the complement of set  $B$ ?

4. Given  $U = \{x \mid x \text{ is a factor of } 20\}$

$O = \{x \mid x \text{ is a factor of } 10\}$

Find  $(O)'$ .

# Interval Notation

Interval Notation is an **alternative to expressing your answer as an inequality.**

**\*\*For the most part, we will use these with compound inequalities.\*\***

Use ( ) \_\_\_\_\_ and [ ] \_\_\_\_\_

**For Example:**

Inequality:  $-4 \leq x \leq 6$

**Interval Notation:**  $[-4, 6]$

Inequality:  $0 < x \leq 20$

**Interval Notation:**  $(0, 20]$

Try These: Write each Inequality in Interval Notation.

1.  $2 < x < 5$

2.  $10 \leq x < 23$

3.  $-5 \leq x \leq -1$

On your Own: **Write the Compound Inequality First.**

1. All numbers between 1 and 5 including the 1 and the 5.

2. All numbers greater than or equal to 5 and less than 12.

3. All numbers greater than 2 but less than or equal to 20.

4. All numbers between -3 and 3, inclusive.