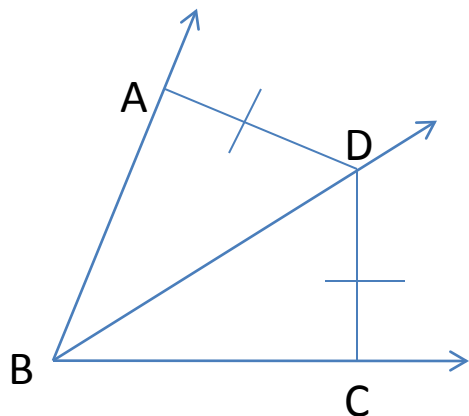


# Angle Bisector and Perpendicular Bisector Theorem

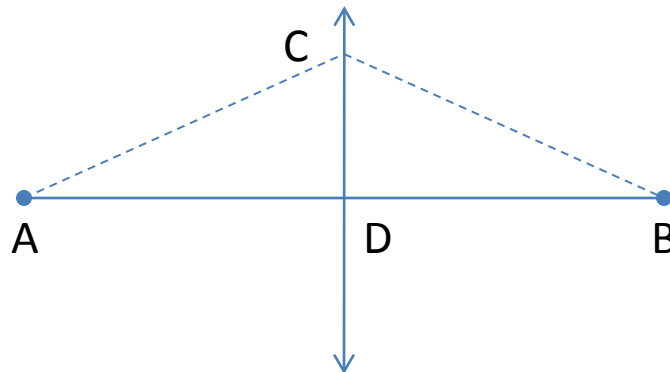
If  $m\angle ABD = 4x - 10$  and  $m\angle CBD = 7x - 31$ , find  $m\angle CBD$



1.

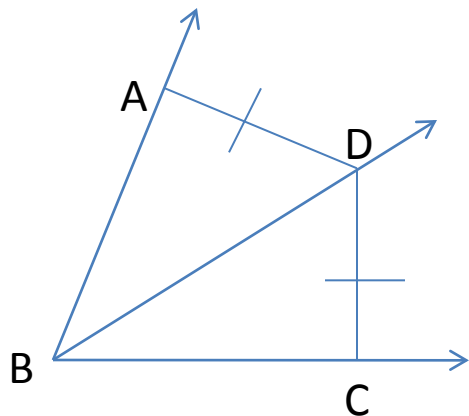
$CD$  is the Perpendicular Bisector of  $AB$

If  $AC = 11x - 50$  and  $CB = 3x + 30$ , find  $AC$



2.

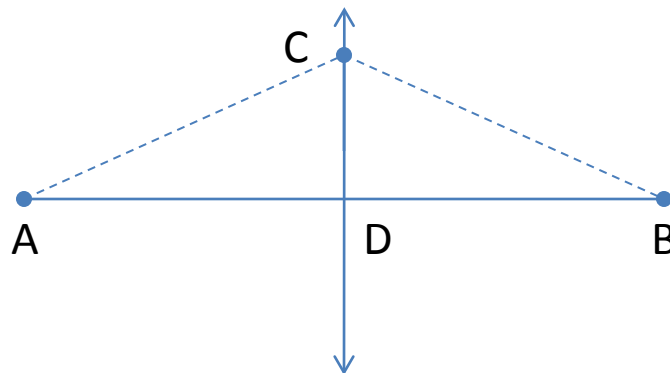
If  $m\angle ABD = 3x + 15$  and  $m\angle CBD = 4x + 4$ , find  $m\angle ABC$



3.

$CD$  is the Perpendicular Bisector of  $AB$

If  $AC = 6x + 9$  and  $CB = 2x + 33$ , find  $CB$



4.

# Angle Bisector and Perpendicular Bisector Theorem (A)

$$m\angle CBD = 18^\circ$$

$$AC = 60$$

1.

2.

$$m\angle ABC = 96^\circ$$

$$CB = 45$$

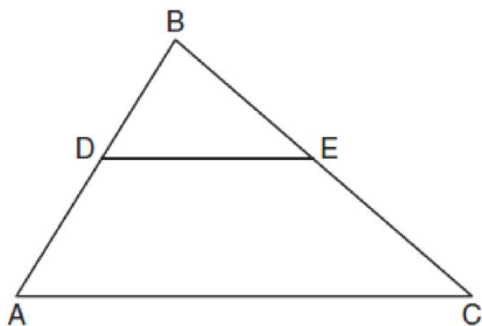
3.

4.

# Triangle Midsegment Theorem #1

D is the Midpoint of AB and E is the Midpoint of BC

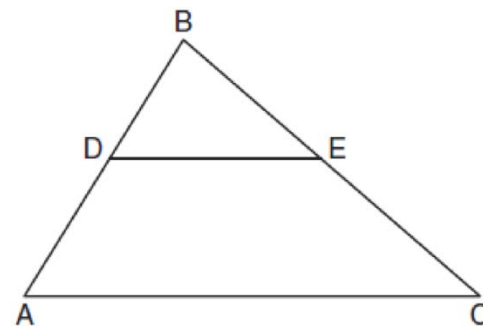
If  $DE = 4x - 9$  and  $AC = 3x + 22$ , find  $DE$



1.

D is the Midpoint of AB and E is the Midpoint of BC

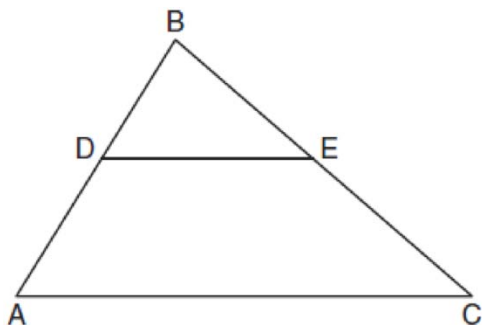
If  $DE = 7x + 1$  and  $AC = 6x + 18$ , find  $AC$



2.

D is the Midpoint of AB and E is the Midpoint of BC

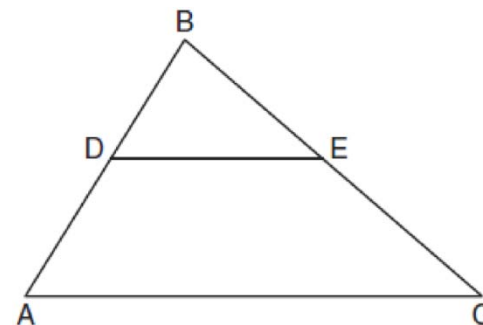
If  $DE = 2x - 16$  and  $AC = 3x - 3$ , find  $DE$



3.

D is the Midpoint of AB and E is the Midpoint of BC

If  $DE = 8x - 10$  and  $AC = 10x + 40$ , find  $AC$



4.

# Triangle Midsegment Theorem #1 (A)

$$DE = 23$$

$$AC = 30$$

1.

2.

$$DE = 42$$

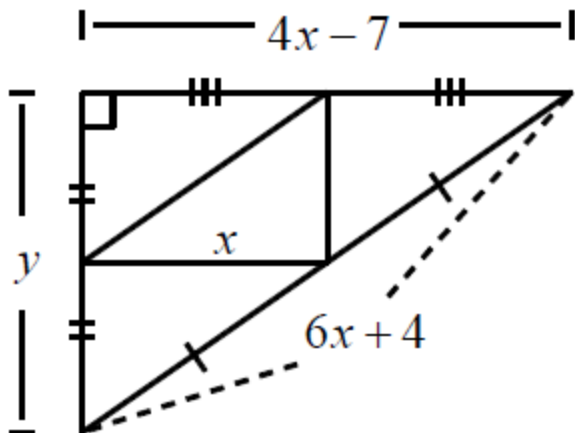
$$AC = 140$$

3.

4.

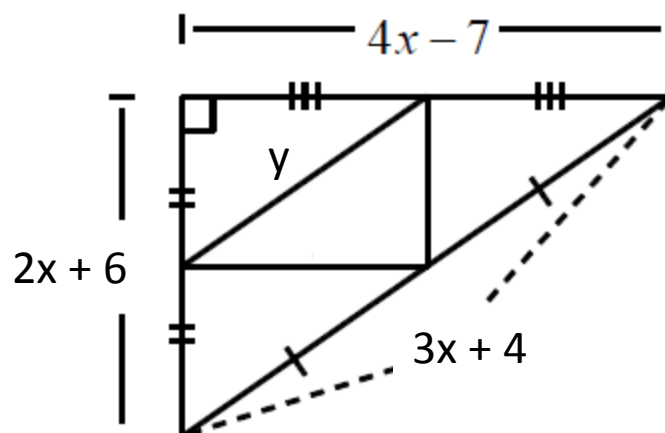
# Triangle Midsegment Theorem #2

If the Perimeter of the Large Triangle is 56, find  $y$ .



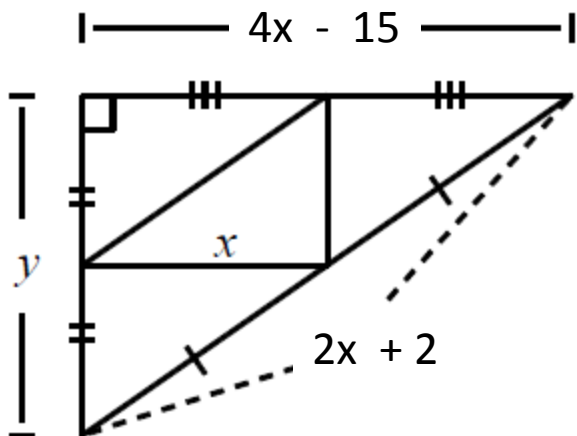
1.

If the Perimeter of the Large Triangle is 30, find  $y$ .



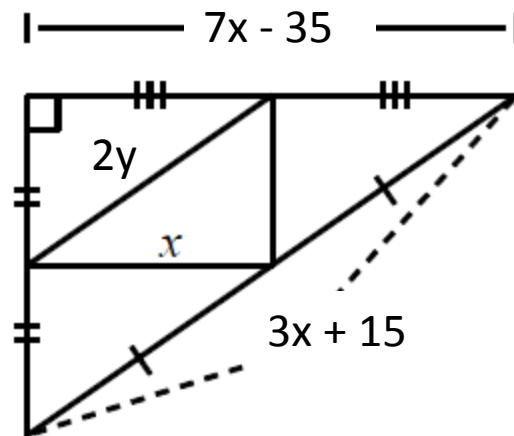
2.

If  $y = 8$ , find the perimeter of the Smaller Triangle



3.

Find  $x$  and  $y$ .



4.

## Triangle Midsegment Theorem #2 (A)

$$y = 24$$

$$y = 6.5$$

1.

2.

$$P = 20$$

$$x = 7$$

$$y = 9$$

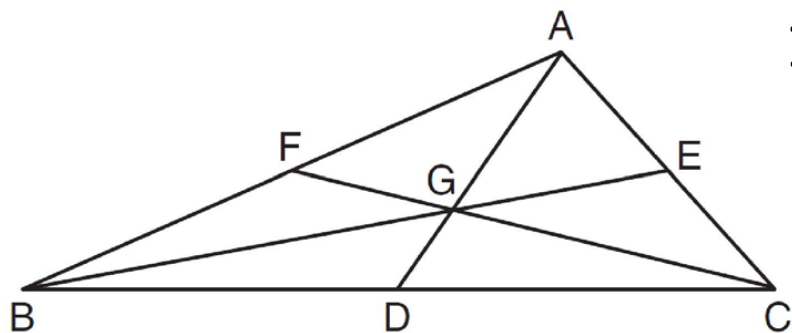
3.

4.

# Two-Thirds (Centroid) Theorem

Given:  $AG = 14$ ,  $FG = 10$ ,  $EB = 36$

Find:  $GD$ ,  $AD$ ,  $CG$ ,  $CF$ ,  $EG$ ,  $BG$

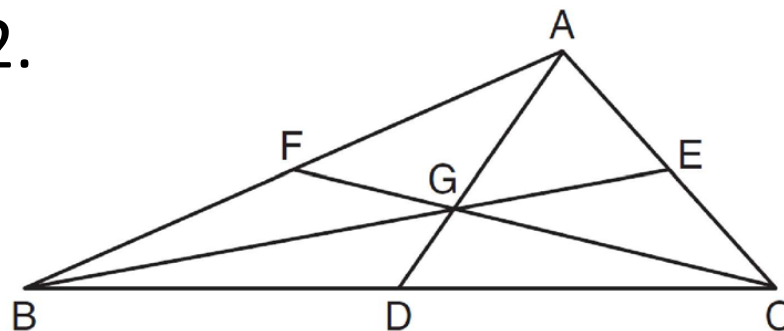


1.

2.

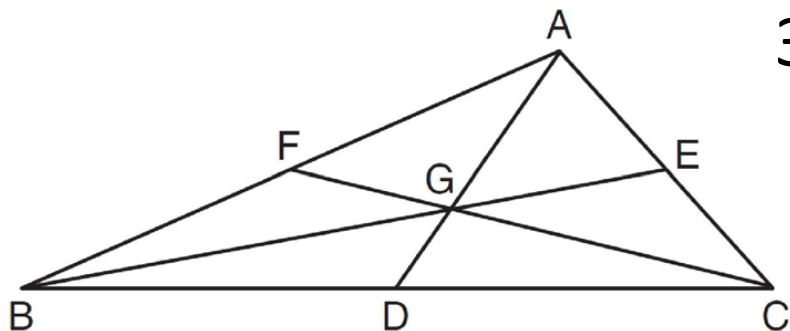
Given:  $AD = 15$ ,  $GE = 19$ ,  $FG = 6$

Find:  $AG$ ,  $GD$ ,  $BG$ ,  $BE$ ,  $CF$ ,  $CG$



Given:  $CF = 9$ ,  $GD = 2$ ,  $BG = 16$

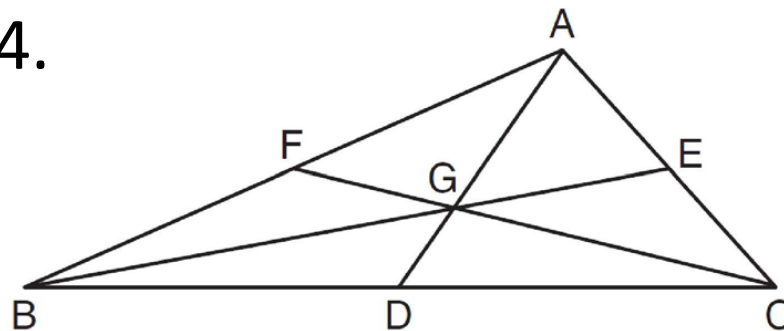
Find:  $CG$ ,  $GF$ ,  $AG$ ,  $AD$ ,  $GE$ ,  $BE$



3.

Given:  $BE = 27$ ,  $DG = 4$ ,  $CG = 10$

Find:  $BG$ ,  $GE$ ,  $GA$ ,  $DA$ ,  $CF$ ,  $GF$



4.

## Two-Thirds (Centroid) Theorem (A)

$$GD = 7, \quad AD = 21, \quad CG = 20,$$

$$CF = 30, \quad EG = 12, \quad BG = 24$$

1.

$$AG = 10, \quad GD = 5, \quad BG = 38,$$

$$BE = 57, \quad CF = 18, \quad CG = 12$$

2.

$$CG = 6, \quad GF = 3, \quad AG = 4,$$

$$AD = 6, \quad GE = 8, \quad BE = 24$$

3.

$$BG = 18, \quad GE = 9, \quad GA = 8,$$

$$DA = 12, \quad CF = 15, \quad GF = 5$$

4.



# Perpendicular/Angle Bisectors, Medians, and Altitudes

The vertices of the triangle in the diagram below are  $A(7,9)$ ,  $B(3,3)$ , and  $C(11,3)$ .

What are the coordinates of the centroid of  $\triangle ABC$ ?

1.

The vertices of the triangle in the diagram below are  $A(0,0)$ ,  $B(4,0)$ , and  $C(4,-3)$ .

Find the center of the circle you can circumscribe about  $\triangle ABC$ .

2.

The vertices of the triangle in the diagram below are  $A(-2,5)$ ,  $B(6,5)$ , and  $C(4,-1)$ .

What are the coordinates of the orthocenter of  $\triangle ABC$ ?

3.

The vertices of the triangle in the diagram below are  $A(-1,-2)$ ,  $B(-5,-2)$ , and  $C(-1,-7)$ .

Find the center of the circle you can circumscribe about  $\triangle ABC$ .

4.

# Perpendicular/Angle Bisectors, Medians, and Altitudes (A)

( 7 , 5 )

( 2 , -1.5 )

1.

2.

( 4 , 3 )

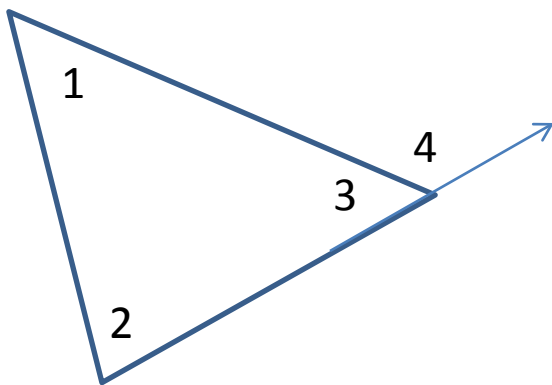
( -3 , -4.5 )

3.

4.

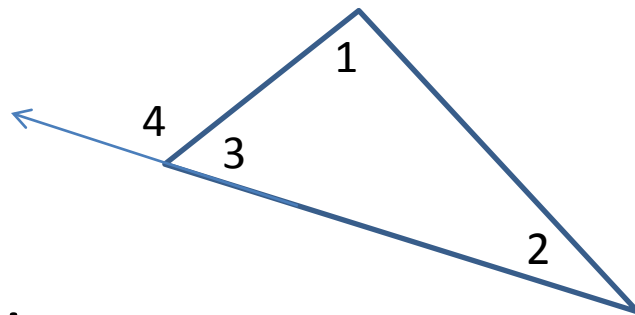
# Triangle Exterior Angle Theorem

If  $m\angle 1 = 4x$ ,  $m\angle 2 = 60$ , and  $m\angle 3 = 6x$  find  $m\angle 4$



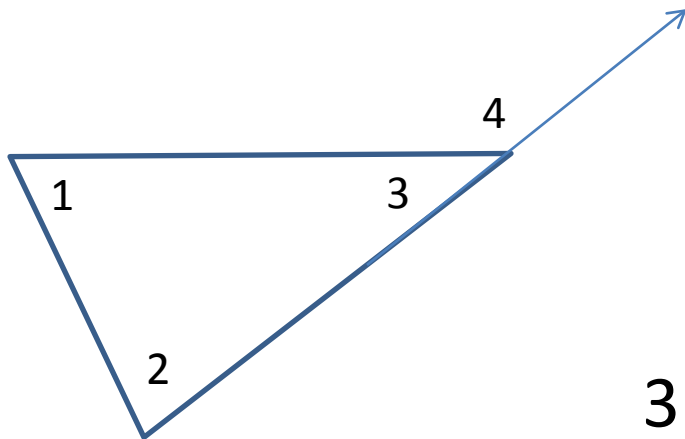
1.

If  $m\angle 1 = x + 40$ ,  $m\angle 2 = 4x - 5$ , and  $m\angle 4 = 6x + 20$  find  $m\angle 1$



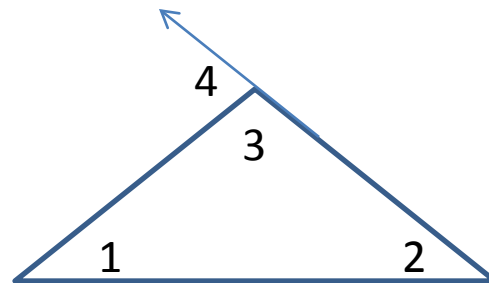
2.

If  $m\angle 1 = 2x + 17$ ,  $m\angle 2 = 3x$ , and  $m\angle 4 = 7x - 33$  find  $m\angle 4$



3.

If  $m\angle 3 = 106$ ,  $m\angle 2 = 2x - 1$ , and  $m\angle 4 = 6x + 2$  find  $m\angle 1$



4.

# Triangle Exterior Angle Theorem (A)

$$m\angle 4 = 108^\circ$$

$$m\angle 1 = 55^\circ$$

1.

2.

$$m\angle 4 = 142^\circ$$

$$m\angle 4 = 51^\circ$$

3.

4.

# Triangle Angle-Side Relationship

In  $\triangle ABC$ ,  $m\angle A = 90$ ,  $m\angle B = 55$ , and  $m\angle C = 35$ .

- a) List the sides in order from smallest to largest.
- b) Classify the triangle by its sides.

1.

In triangle  $ABC$ ,  $m\angle B = 140$  and  $m\angle C = 20$ .

- a) List the sides in order from smallest to largest.
- b) Classify the triangle by its angles.

2.

In  $\triangle PQR$ ,  $PQ = 8$ ,  $QR = 12$ , and  $RP = 13$ .

- a) List the angles in order from smallest to largest.
- b) Classify the triangle by its sides.

3.

In  $\triangle ABC$ , measure of  $\angle ACB = 70^\circ$  and the measure of  $\angle ABC = 65^\circ$ .

- a) List the sides in order from smallest to largest.
- b) Classify the triangle by its angles.

4.

# Triangle Angle-Side Relationship (A)

a)  $AB, AC, BC$

b) Scalene Triangle because all angles are different measures therefore all sides will be different measure.

1.

a)  $AB = BC, AC$

b) Obtuse Triangle because it contains an angle greater than  $90^\circ$ .

2.

a)  $\angle R, \angle P, \angle Q$

b) Scalene Triangle because all sides are different measures therefore all sides will be different measure.

3.

a)  $BC, AC, AB$

b) Acute Triangle because all angles are less than  $90^\circ$ .

4.

# Triangle Inequality Theorem

Sara is building a triangular pen for her pet rabbit. If two of the sides measure 8 feet and 15 feet, write an inequality to determine the possible length of the third side.

1.

If the lengths of two sides of a triangle are 4 and 10, what could be the length of the third side?

2.

José wants to build a triangular pen for his pet rabbit. He has three lengths of boards already cut that measure 7 feet, 8 feet, and 16 feet. Explain why José cannot construct a pen in the shape of a triangle with these sides.

3.

Jesse is building a triangular pen for her pet squirrel. If two of the sides measure 10 feet and 20 feet, write an inequality to determine the possible length of the third side.

4.

# Triangle Inequality Theorem (A)

$$7 < x < 23$$

$$6 < x < 14$$

1.

2.

$7 + 8 = 15$  and the sum of the two shorter sides of a triangle must be greater than the third side.

$$10 < x < 30$$

3.

4.