

7-4 System of Equations Word Problems

Pam is playing with red and black marbles. She has 42 marbles in all. The number of red marbles she has is three more than twice the number of black marbles she has. How many of each color marble does Pam have? Let r = red b = black

$$\begin{aligned} r + b &= 42 \\ r &= 2b + 3 \end{aligned}$$

13 black marbles
29 red marbles

$$\begin{aligned} 2b + 3 + b &= 42 \\ 3b + 3 &= 42 \\ -3 &-3 \\ \hline 3b &= 39 \\ 3 &3 \\ \hline b &= 13 \end{aligned}$$

$$b = 13$$

$$r = 29$$

$$\begin{aligned} r + b &= 42 \\ r + 13 &= 42 \\ -13 &-13 \\ \hline r &= 29 \end{aligned}$$

2. Top Tunes sells CD's and tapes. Brianna bought 3 CDs and 2 tapes for \$58. Ramon bought 1 CD and 4 tapes for \$46. Determine the selling price for 1 CD and 1 tape.

$c \rightarrow$ \$CD $t \rightarrow$ \$tape

$$\begin{aligned} -2(3c + 2t &= 58) \rightarrow -6c - 4t = -116 \\ 1c + 4t &= 46 \rightarrow 1c + 4t = 46 \end{aligned}$$

CD costs \$14.00
Tape costs \$8.00

$$\begin{aligned} -6c - 4t &= -116 \\ 1c + 4t &= 46 \\ \hline -5c &= -70 \\ -5 &-5 \\ \hline c &= 14 \end{aligned}$$

$$\begin{aligned} 3c + 2t &= 58 \\ 3(14) + 2t &= 58 \\ 42 + 2t &= 58 \\ -42 &-42 \\ \hline 2t &= 16 \\ 2 &2 \\ \hline t &= 8 \end{aligned}$$

3. Jack bought 3 slices of cheese pizza and 4 slices of mushroom pizza for a total cost of \$12.50. Grace bought 3 slices of cheese pizza and 2 slices of mushroom pizza for a total cost of \$8.50. Determine the selling price for one slice of cheese and one slice of mushroom.

$c =$ \$cheese pizza $m =$ \$mushroom pizza

$$\begin{aligned} 3c + 4m &= 12.50 \rightarrow 3c + 4m = 12.50 \\ -1(3c + 2m &= 8.50) \rightarrow -3c - 2m = -8.50 \end{aligned}$$

Cheese pizza = \$1.50
mushroom pizza = \$2.00

$$\begin{aligned} 3c + 4m &= 12.50 \\ -3c - 2m &= -8.50 \\ \hline 2m &= 4.00 \\ 2 &2 \\ \hline m &= 2.00 \end{aligned}$$

$$\begin{aligned} 3c + 4m &= 12.50 \\ 3c + 4(2.00) &= 12.50 \\ 3c + 8 &= 12.50 \\ -8 &-8 \\ \hline 3c &= 4.50 \\ c &= 1.50 \end{aligned}$$

4. Erin has \$0.80 in nickels and dimes. She has 12 coins in all. Find how many nickels and dimes Erin has by using a system of equations?

$n \rightarrow$ nickels

$d \rightarrow$ dimes

$$\begin{aligned} -0.05(n + d &= 12) \rightarrow -0.05n - 0.05d = -0.60 \\ 0.05n + 0.10d &= 0.80 \end{aligned}$$

nickels = 8, dimes = 4

$$\begin{aligned} -0.05n - 0.05d &= -0.60 \\ 0.05n + 0.10d &= 0.80 \\ \hline 0.05d &= 0.2 \end{aligned}$$

$$\begin{aligned} d &= 4 \\ n &= 8 \end{aligned}$$

Homework

Practice 7-4

Name _____

1. Solve the following system of equation by Elimination

$$3x + 4y = 12.50$$

$$3x + 2y = 8.50$$

2. Sam and Odel have been selling frozen pizzas for a class fundraiser. Sam has sold half as many pizzas as Odel. Together they have sold a total of 126 pizzas. How many pizzas did Sam sell?

3. The cost of 3 markers and 2 pencils is \$1.80. The cost of 4 markers and 6 pencils is \$2.90. What is the cost of *each* item? Include appropriate units in your answer.