

## 12-5 Adding and Subtracting Rational Expressions

### Adding and Subtracting with Common Denominators

Rule: add/subtract numerators

KEEP denominator

$$\frac{3}{10} + \frac{6}{10} = \frac{9}{10}$$

$$\frac{8x}{13} - \frac{4x}{13} = \frac{4x}{13}$$

$$\frac{x}{x+2} + \frac{5}{x+2} = \frac{\cancel{x+2}}{\cancel{x+2}} \quad \text{the same}$$

### Adding Then Simplifying

$$1. \frac{5x-10}{6} + \frac{x-2}{6} = \frac{6x-12}{6}$$

$$2. \frac{x^2}{x+3} + \frac{11x+24}{x+3} = \frac{x^2+11x+24}{x+3}$$

$$1x - 2$$

$$\cancel{x-2}$$

$$\frac{\cancel{(x+3)(x+8)}}{\cancel{x+3}}$$

$$\frac{1}{x+8}$$

### Subtracting Then Simplifying

$$3. \frac{6x+1}{3x} - \frac{3x+4}{3x} = \frac{3x-3}{3x}$$

$$\frac{3(x-1)}{3x}$$

$$\cancel{\frac{x-1}{x}}$$

$$4. \frac{9x}{2x+7} - \frac{x-28}{2x+7} = \frac{8x+28}{2x+7}$$

$$\frac{4(2x+7)}{\cancel{(2x+7)}}$$

$$\frac{4}{\cancel{4}}$$

## Adding and Subtracting with UN-Common Denominators

**Rule:** GET COMMON DENOMINATORS

$$\frac{1}{6} + \frac{3}{4} =$$

$$\frac{1}{6} \cdot 2 = \frac{2}{12}$$

$$\frac{3}{4} \cdot 3 = \frac{9}{12}$$

LCD:

$$\frac{2}{12} + \frac{9}{12} = \frac{11}{12}$$

$$\frac{5}{10} - \frac{x}{5x} =$$

$$\begin{aligned} \frac{5}{10} &\cdot x = \frac{5x}{10x} \\ \frac{x}{5x} &\cdot 2 = \frac{2x}{10x} \end{aligned}$$

LCD:

$$\frac{5x}{10x} - \frac{2x}{10x} = \frac{3x}{10x}$$

$$= \frac{3}{10}$$

**Adding Then Simplifying**

$$\frac{6}{5x^8} + \frac{4}{3x^8} =$$

$$\frac{6}{5x^8} \cdot 3 = \frac{18}{15x^8}$$

$$\frac{4}{3x^8} \cdot 5 = \frac{20}{15x^8}$$

LCD:

$$\begin{aligned} \frac{18}{15x^8} + \frac{20}{15x^8} \\ = \frac{38}{15x^8} \end{aligned}$$

$$\frac{5-2x}{3x} + \frac{12-4x}{6x} =$$

$$\begin{aligned} (5-2x) \cdot 2 &= 10-4x \\ 3x \cdot 2 &= 6x \end{aligned}$$

LCD:

$$\frac{10-4x}{6x} + \frac{12-4x}{6x}$$

$$\begin{aligned} \frac{12-4x}{6x} &= \frac{12-4x}{6x} \\ &= \frac{22-8x}{6x} \end{aligned}$$

**Subtracting Then Simplifying**

$$\frac{3}{8x} - \frac{1}{12} =$$

LCD:

$$\frac{x}{x-4} - \frac{24}{(x+2)(x-4)} =$$

LCD:

$$\begin{aligned} 2(x-4) &= 2x-8 \\ 6x &= 6x \\ \frac{11-4x}{3x} &= \end{aligned}$$

## Practice 12-5

Name \_\_\_\_\_

1. What is  $\frac{2+x}{5x} - \frac{x-2}{5x}$  expressed in simplest form?

2. What is the sum of  $\frac{3x^2}{x-2}$  and  $\frac{x^2}{x-2}$ ?

3. What is the sum of  $\frac{-x+7}{2x+4}$  and  $\frac{2x+5}{2x+4}$ ?

4. What is  $\frac{x^3}{x+3} - \frac{9x}{x+3}$  expressed in simplest form?

5. What is the result, in simplest form, when  $\frac{4x-5}{x^2-64}$  is subtracted from  $\frac{5x+3}{x^2-64}$

6. What is the sum of  $\frac{3}{2x}$  and  $\frac{7}{4x}$ ?

7. What is the difference of  $\frac{6}{5x}$  and  $\frac{2}{3x}$ ?

8. Subtract and simplify  $\frac{x-7}{6} - \frac{3x-2}{12}$

9. Express in simplest form:  $\frac{5x+3}{x} - \frac{x-1}{2x}$

10. What is the sum of  $\frac{-4+x}{5x}$  and  $\frac{-3x-2}{4x}$ ?